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# Retrieval of tropospheric column-averaged CH<sub>4</sub> mole fraction by solar absorption FTIR-spectrometry using N<sub>2</sub>O as a proxy

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## Abstract

Tropospheric column-averaged CH<sub>4</sub> mole fractions were derived from ground-based absorption columns measurements. The method used stratospheric N<sub>2</sub>O columns to correct for the stratospheric contribution to the CH<sub>4</sub> total column. The method was applied to four TCCON sites covering locations from the Northern Arctic to the tropics. It performs well for all sites. The derived tropospheric CH<sub>4</sub> concentrations were compared with profiles measured by aircraft at three sites. The results indicate an inter-site consistency within 6 ppb (~ 0.3 %). With aircraft profiles up to 3 km, the seasonal behavior of the derived tropospheric CH<sub>4</sub> concentration was also checked. It reveals a difference of 20 ppb around. The mean relative uncertainty of the four sites is 0.23 %. Comparing with the method using HF the proposed method shows a smaller relative uncertainty and less H<sub>2</sub>O dependence.

## 1 Introduction

Methane (CH<sub>4</sub>) is the second most important anthropogenic greenhouse gas in the atmosphere (Montzka et al., 2011). The main sources of CH<sub>4</sub> to the atmosphere are natural wetlands, anthropogenic activities (livestock production; rice cultivation; production, storage, transmission, and distribution of fossil fuels; waste waters and landfills) and biomass burning. The destruction by OH in the troposphere is the dominant atmospheric sink of CH<sub>4</sub>. Both anthropogenic and natural emissions of CH<sub>4</sub> are likely to increase in the twenty-first century as global population increases and climate warms. The atmospheric mole fraction of methane has increased from about 700 ppb to the current atmospheric background of about 1800 ppb since 1770. Despite this dramatic increase, the observed global annual mean atmospheric abundance was nearly constant from 1999 to 2006, before it began to increase again in 2007 (Rigby et al., 2008; Dlugokencky et al., 2009). This behaviour is a subject of open scientific discussion (Bousquet et al., 2011; Pison et al., 2013).

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Atmospheric CH<sub>4</sub> concentrations measurements can be linked quantitatively to regional sources and sinks by inverse modeling. Improving both the quality and quantity of measurements is a way to better constrain source and sinks, since it is an under-constrained problem. The Total Carbon Column Observation Network (TCCON) was founded to remotely measure column abundances of CO<sub>2</sub>, CH<sub>4</sub>, CO, N<sub>2</sub>O and other molecules that absorb in the near infrared (NIR) (Wunch et al., 2011). The Network for the Detection of Atmospheric Composition Change (NDACC) ground-based solar absorption spectrometry in mid infrared (MIR) spectral regions can provide total column measurement for many gases (Sussmann et al., 2013). Such column data are essential for the validation of greenhouse gas measurements from satellites and as input or independent validation for inverse model studies. The column-averaged dry-air mole fraction (DMF) of CH<sub>4</sub> (known as  $X_{\text{CH}_4}$ ) can be determined by ratioing to the retrieved column of the reference gas O<sub>2</sub>, whose atmospheric abundance is well known. The tropospheric column-averaged mole fraction of CH<sub>4</sub> can be derived using methods based on: (i) a posteriori correction using a proxy for variations in the stratospheric contribution to the total column, such as the HF total column as an estimator for the stratospheric CH<sub>4</sub> contribution (Washenfelder et al., 2003; Warneke et al., 2006); and (ii) direct determination of the tropospheric mole fraction of CH<sub>4</sub> via retrieval of CH<sub>4</sub> profiles (Sepúlveda et al., 2012). Currently the second method is only applied to NDACC high-resolution MIR solar absorption spectra, not to the NIR TCCON spectra. The first method is based on the fact that HF is solely present in the stratosphere and a linear relationship exists between the DMFs of the CH<sub>4</sub> and HF with respect to changes in tropopause height. The stratospheric column of the CH<sub>4</sub> can therefore be inferred from the total column of the HF via this linear relationship, and then subtracted from the total column of the CH<sub>4</sub> to yield the tropospheric CH<sub>4</sub> column. Variations in the CH<sub>4</sub> column due to changes in surface pressure are determined from the O<sub>2</sub> column. Using this method, the tropospheric column-averaged DMF of CH<sub>4</sub> can be determined with a precision of 0.5 % (Washenfelder et al., 2003).







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the ACE-FTS satellite (Bernath et al., 2005). For the derivation of  $a$  and  $b$ , the retrieved stratospheric profiles of HF, N<sub>2</sub>O and CH<sub>4</sub> are separated into several 20° wide latitude bands. In case of HF, the latitudinal variation of the slope  $b$  ranges from 740 ~ 870 ppb ppb<sup>-1</sup>, and from 3.6 to 4.4 ppb ppb<sup>-1</sup> for N<sub>2</sub>O. Between 2004 and 2010 no discernable time-dependency could be detected. For the four TCCON sites: Spitsbergen, Bialystok, Orléans and Darwin their corresponding slopes  $b$  for their corresponding latitude bands are 4.34, 4.39, 4.39 and 3.53 respectively for N<sub>2</sub>O, and -749.05, -751.21, -751.21 and -876.03 for HF.

Here, we employ two strategies to retrieve the tropospheric column-averaged CH<sub>4</sub> mole fraction. Each one is described below: one strategy explicitly uses tropopause pressure to correct for the contribution of stratospheric CH<sub>4</sub> and the other one relies on the variation of HF or N<sub>2</sub>O to implicitly derive the tropopause height.

### 3.1 Strategy explicitly using tropopause pressure

Multiplying both sides of Eq. (1) with air density and integrating it over the stratosphere yields,

$$VC_{CH_4}^{strat} = a \cdot VC_{air}^{strat} + b \cdot VC_y^{strat} \quad (2)$$

where VC denotes the vertical column. The stratospheric column of  $y$  can be obtained by subtracting the tropospheric column from the total column, so Eq. (2) can be rewritten as follows:

$$VC_{CH_4}^{strat} = a \cdot VC_{air}^{strat} + b (VC_y - VC_y^{trop}) \quad (3)$$

The tropospheric column-averaged mole fraction of the CH<sub>4</sub> is then calculated as:

$$X_{CH_4}^{trop} = \frac{VC_{CH_4} - VC_{CH_4}^{strat}}{VC_{air}^{trop}} \quad (4)$$



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b. Since we can assume that the N<sub>2</sub>O mole fraction is a constant known quite well and the HF mole fraction is zero throughout the troposphere, we can calculate the constant *a* if we know the CH<sub>4</sub> mole fraction at tropopause. This is done iteratively, starting from the constant *a* derived from satellite measurements and then using Eqs. (3) and (4) to calculate the tropospheric column-averaged CH<sub>4</sub> mole fraction. Since we need to know the CH<sub>4</sub> mole fraction at the tropopause the relative distribution profile of CH<sub>4</sub> mole fraction in the troposphere is needed. Here the GFIT a priori profile is assumed. Then this profile of CH<sub>4</sub> is scaled so that the tropospheric column-averaged CH<sub>4</sub> mole fraction calculated from the scaled a priori profile is equal to that derived using Eqs. (3) and (4). Then the mole fraction value of the scaled a priori CH<sub>4</sub> profile at tropopause is used to calculate the new value of the constant *a*. This process is repeated until that the change in the constant *a* is overlooked. Figure 2 gives a comparison between constant *a* derived from the original and scaled GFIT a priori and the satellite data at Spitsbergen.

According to the results of Eqs. (5) and (6), the relative fractions of tropospheric and stratospheric dry air column can be determined. The total dry air column inferred from the O<sub>2</sub> column is then separated into tropospheric and stratospheric parts according to these fractions. The dry air columns in the stratosphere and troposphere derived from O<sub>2</sub> column are used in Eqs. (3) and (4). Although surface pressure can be measured with better precision than the O<sub>2</sub> column, using O<sub>2</sub> column takes into account factors that affect CH<sub>4</sub>, N<sub>2</sub>O, HF and O<sub>2</sub> column retrievals in a common way – pointing/tracking, any light path variations etc. In the calculation above, the water vapor is assumed to be located completely in the troposphere. We also tested the assumption that the retrieved water vapor profile is vertically distributed as described in the a priori (that is, according to the NCEP profile). The two methods produce a difference of less than 0.5 ppb in the derived tropospheric column-averaged mole fraction of CH<sub>4</sub>, so for simplicity the first method is applied.

### 3.2 Strategy implicitly using tropopause pressure

In the case of the HF, when approaching the tropopause, the HF mole fraction approaches zero and so the constant  $a$  in Eq. (1) represents  $\text{CH}_4$  mole fraction around the tropopause. Washenfelder et al. (2003) consider  $a$  as the tropospheric column-averaged  $\text{CH}_4$  mole fraction, and use  $\text{O}_2$  to infer the dry air column. Under these conditions, inserting Eq. (3) into Eq. (4) yields the equation used by them,

$$X_{\text{CH}_4}^{\text{trop}} = a = \frac{0.2095(\text{VC}_{\text{CH}_4} - b \cdot \text{VC}_{\text{HF}})}{\text{VC}_{\text{O}_2}} \quad (7)$$

This method can be used for  $\text{N}_2\text{O}$  as well. Since in the troposphere, the  $\text{N}_2\text{O}$  mole fraction is almost constant and its value can be quite well predicted, we then subtract the tropospheric  $\text{N}_2\text{O}$  mole fraction from its mole fraction profile in the whole atmosphere. Such a derived “species” will also be present completely in the stratosphere and Eq. (1) also holds as long as the constant  $a$  is replaced by a value equal to  $a$  plus the tropospheric  $\text{N}_2\text{O}$  mole fraction multiplied by the slope  $b$ , and consider this quantity as the tropospheric column-averaged  $\text{CH}_4$  mole fraction. We obtain the following equation,

$$X_{\text{CH}_4}^{\text{trop}} = \frac{\text{VC}_{\text{CH}_4} - b \left( \text{VC}_y - X_y^{\text{trop}} \text{VC}_{\text{O}_2} / 0.2095 \right)}{\text{VC}_{\text{O}_2} / 0.2095} \quad (8)$$

$X_y^{\text{trop}}$  is replaced by  $X_{\text{N}_2\text{O}}^{\text{trop}}$  for  $\text{N}_2\text{O}$  or set to zero for HF. Compared with the strategy in Sect. 3.1, this approach does not use the tropopause pressure to correct for the stratospheric contribution of  $\text{CH}_4$  column. The tropopause pressure used here is derived from the NCEP temperature profile and is therefore the thermal tropopause and not necessarily the same as the chemical tropopause. Variation of the location of thermal tropopause from the chemical tropopause will distort the assumption about the vertical distribution of  $\text{N}_2\text{O}$  and HF. In the implicit strategy, the stratospheric contribution is inferred from variations of the  $\text{N}_2\text{O}/\text{HF}$  column, which mainly results from variation of the

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chemical tropopause. So the implicit strategy is free from the influence of inaccuracy in tropopause pressure.

### 3.3 Accounting for the averaging kernel effect

Due to the effect of the averaging kernel the straightforward equations above (Eqs. 4 and 8) need to be modified. The total column retrieved by GFIT is a weighted summation of partial columns at different altitudes. The weights are represented by the averaging kernel and a pressure weighting function that usually differs from one. The partial column reflected in the retrieved total column will be very different from its original value. Figure 3 presents the averaging kernels of HF, N<sub>2</sub>O and CH<sub>4</sub> for Bialystok from all spectra during 2010. The averaging kernel mainly depends on the solar zenith angle. In the case of N<sub>2</sub>O, the averaging kernel has a large weight in stratosphere and small weight in troposphere, so variations in the stratospheric column of N<sub>2</sub>O will be amplified in the retrieved total column compared to the true atmospheric variability, and tropospheric variations will be dampened. For CH<sub>4</sub>, the averaging kernel is close to unity at all altitudes, so the effect of the averaging kernel is small. From Rodgers (2000) and Wunch et al. (2010) the mole fraction profile retrieved by a profile-scaling retrieval, such as that performed by GFIT, is:

$$x_r = x_a + A(x_t - x_a) \quad (9)$$

where, the  $x_r$ ,  $x_t$  and  $x_a$  are the retrieved, true and a priori mole fraction profile, respectively.  $A$  is the averaging kernel. Integrating Eq. (10) and rearranging yields:

$$\int_0^{P_s} x_r \frac{dp}{mg} = \int_0^{P_s} (I - A)x_a \frac{dp}{mg} + \int_0^{P_s} A \left( x_t^{\text{strat}} + x_t^{\text{trop}} \right) \frac{dp}{mg} \quad (10)$$

where,  $m$  is the molecular mass of moist air (i.e.  $m = (1 - x_{\text{H}_2\text{O}}) m_{\text{dry}}^{\text{air}} + x_{\text{H}_2\text{O}} \cdot m_{\text{H}_2\text{O}}$ ),  $g$  is the gravitational acceleration and  $I$  is the identity matrix. In Eq. (10), the true mole

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fraction profile is separated into stratospheric and tropospheric components. Because GFIT performs a profile scaling retrieval and produces the column averaging kernel vector (Connor, 2009) instead of a full averaging kernel matrix, when using a column averaging kernel Eq. (10) can be rewritten as:

$$5 \int_0^{P_s} x_r \frac{dp}{mg} = \int_0^{P_s} (1 - a(p)) x_a \frac{dp}{mg} + \int_{P_t}^{P_s} a(p) x_t \frac{dp}{mg} + \int_0^{P_t} a(p) x_t \frac{dp}{mg} \quad (11)$$

where  $a(p)$  is the column averaging kernel vector, which is a function of pressure (altitude). It can be seen from the equation above that there are three terms contributing to the retrieved total column: the a priori profile, and the tropospheric and stratospheric columns. We then define the following relationships:

$$10 \alpha = \frac{\int_{P_t}^{P_s} x_t \frac{dp}{mg}}{\int_{P_t}^{P_s} a(p) x_t \frac{dp}{mg}} \quad (12)$$

$$\beta = \frac{\int_0^{P_t} x_t \frac{dp}{mg}}{\int_0^{P_t} a(p) x_t \frac{dp}{mg}} \quad (13)$$

$$15 \gamma = \int_0^{P_s} (1 - a(p)) x_a \frac{dp}{mg} \quad (14)$$

$\alpha$  is the ratio of the true tropospheric column to that reflected in the retrieved column,  $\beta$  has a same meaning for the stratosphere, and  $\gamma$  is the a priori part of the retrieved column. To account for the effect of the averaging kernel, Eqs. (3) and (4) are be modified

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to give:

$$VC_{CH_4}^{strat} = a \cdot VC_{air}^{strat} + b \cdot \beta_y (VC_y - VC_y^{trop} \cdot \alpha_y^{-1} - \gamma_y) \quad (15)$$

$$X_{CH_4}^{trop} = \frac{\alpha_{CH_4} (VC_{CH_4} - VC_{CH_4}^{strat} \cdot \beta_{CH_4}^{-1} - \gamma_{CH_4})}{VC_{air}^{trop}} \quad (16)$$

5 In Eq. (15), multiplying  $VC_y^{trop}$  by the inverse of  $\alpha_y$  takes retrieval sensitivity of  $y$  in the tropospheric part into account. Subtracting  $VC_y^{trop} \cdot \alpha_y^{-1}$  and  $\gamma_y$  from the retrieved total column  $VC_y$  yields the stratospheric column of  $y$  reflected in its retrieved total column. Then multiplying by  $\beta_y$  removes retrieval sensitivity in the stratospheric column of  $y$ . In Eq. (16), multiplying  $VC_{CH_4}^{strat}$  by the inverse of  $\beta_{CH_4}$  takes retrieval sensitivity

10 of  $CH_4$  to the stratospheric part into account. Subsequently subtracting  $VC_{CH_4}^{strat} \cdot \beta_{CH_4}^{-1}$  and  $\gamma_{CH_4}$  from the retrieved total column gives the tropospheric column reflected in the retrieved column, and multiplying it with  $\alpha_{CH_4}$  removes retrieval sensitivity in the tropospheric column of  $CH_4$ . These coefficients  $\alpha$  and  $\beta$  depend on the shape of true mole fraction profile, which is unknown. So the a priori profile is used to calculate

15 the approximate value of these coefficients. The effectiveness of removing or taking retrieval sensitivity into account in the manipulation above will depend on the difference between the shapes of the true and a priori mole fraction profiles. This could introduce additional error.

The error introduced by using Eqs. (3) and (4) is the smoothing error in the total column, and that using the Eqs. (15) and (16) is the error of the coefficients  $\alpha$  and  $\beta$ . It can be explained as follows, in Eq. (3) the total column of  $y$  can be expressed as:

$$VC_y = \int_0^{P_s} x_t^y \frac{dp}{mg} + \int_0^{P_s} (1 - a_y(p)) (x_a^y - x_t^y) \frac{dp}{mg} \quad (17)$$

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The second term on the right of Eq. (17) is the smoothing error. Inserting Eq. (17) into Eq. (3) yields:

$$VC_{CH_4}^{strat} = a \cdot VC_{air}^{strat} + b \left( \int_0^{P_s} x_t^y \frac{dp}{mg} + \int_0^{P_s} (1 - a_y(p)) (x_a^y - x_t^y) \frac{dp}{mg} - VC_y^{trop} \right) \quad (18)$$

Without accounting for the error in the tropospheric column of  $y$ , the term in brackets on the right of Eq. (18) is just the true stratospheric column of  $y$  plus the smoothing error. For Eq. (15), where the equation accounts for the averaging kernel effect, when the a priori profile is used to calculate the coefficients  $\alpha$  and  $\beta$  it can be rewritten as:

$$VC_{CH_4}^{strat} = a \cdot VC_{air}^{strat} + b \cdot \frac{\int_0^{P_t} x_a^y \frac{dp}{mg}}{\int_0^{P_t} a_y(p) x_a^y \frac{dp}{mg}} \left( VC_y - VC_y^{trop} \cdot \frac{\int_{P_t}^{P_s} a_y(p) x_a^y \frac{dp}{mg}}{\int_{P_t}^{P_s} x_a^y \frac{dp}{mg}} - \gamma_y \right) \quad (19)$$

Inserting Eq. (17) into Eq. (19) and overlooking the error in the tropospheric column of  $y$  yields:

$$VC_{CH_4}^{strat} = a \cdot VC_{air}^{strat} + b \cdot \left( \frac{\int_0^{P_t} x_t^y \frac{dp}{mg}}{\int_0^{P_t} a_y(p) x_t^y \frac{dp}{mg}} + e_1 \right) \left[ \int_0^{P_s} a_y(p) x_t^y \frac{dp}{mg} - \int_{P_t}^{P_s} x_t^y \frac{dp}{mg} \cdot \left( \frac{\int_{P_t}^{P_s} a_y(p) x_t^y \frac{dp}{mg}}{\int_{P_t}^{P_s} x_t^y \frac{dp}{mg}} + e_2 \right) \right] \quad (20)$$

Where  $e_1$  and  $e_2$  are the errors related to the coefficients  $\alpha$  and  $\beta$ ,

$$e_1 = \frac{\int_0^{P_t} x_a^y \frac{dp}{mg}}{\int_0^{P_t} a_y(p) x_a^y \frac{dp}{mg}} - \frac{\int_0^{P_t} x_t^y \frac{dp}{mg}}{\int_0^{P_t} a_y(p) x_t^y \frac{dp}{mg}} \quad (21)$$

$$e_2 = \frac{\int_{P_t}^{P_s} a_y(\rho) x_a^y \frac{d\rho}{mg}}{\int_{P_t}^{P_s} x_a^y \frac{d\rho}{mg}} - \frac{\int_{P_t}^{P_s} a_y(\rho) x_t^y \frac{d\rho}{mg}}{\int_{P_t}^{P_s} x_t^y \frac{d\rho}{mg}} \quad (22)$$

Rearranging the terms in Eq. (20) produces,

$$VC_{CH_4}^{strat} = a \cdot VC_{air}^{strat} + b \cdot \left( \int_0^{P_t} x_t^y \frac{d\rho}{mg} + \int_0^{P_t} a_y(\rho) x_t^y \frac{d\rho}{mg} \cdot e_1 - \int_{P_t}^{P_s} x_t^y \frac{d\rho}{mg} \cdot \frac{\int_0^{P_t} x_a^y \frac{d\rho}{mg}}{\int_0^{P_t} a_y(\rho) x_a^y \frac{d\rho}{mg}} \cdot e_2 \right) \quad (23)$$

- 5 Similar to Eq. (18), the term in brackets is the true stratospheric column of  $y$  plus an error term that is different from the smoothing error. The smoothing error depends on the difference between the shapes of true mole fraction profile and the a priori, and also the overall inhomogeneity of the averaging kernel in the whole atmosphere. The smoothing error increases with an increase in the inhomogeneity of the averaging
- 10 kernel. However the error term in Eq. (23) depends on  $e_1$  and  $e_2$ , which depend on the inhomogeneity of the averaging kernel and the difference between the shapes of the true and a priori mole fraction profiles in only the stratosphere and troposphere, respectively. It can be seen more clearly using another form:

$$e_2 = \frac{\int_{P_t}^{P_s} \int_{P_t}^{P_s} [a_y(\rho_1) - a_y(\rho_2)] x_a^y(\rho_1) x_t^y(\rho_2) \frac{d\rho_1}{mg} \frac{d\rho_2}{mg}}{\int_{P_t}^{P_s} \int_{P_t}^{P_s} x_a^y(\rho_1) x_t^y(\rho_2) \frac{d\rho_1}{mg} \frac{d\rho_2}{mg}} \quad (24)$$

- 15 In Eq. (24), the term  $[a_y(\rho_1) - a_y(\rho_2)]$  is an anti-symmetric function about line  $\rho_1 = \rho_2$  on plane  $(\rho_1, \rho_2)$  and term  $x_a^y(\rho_1) x_t^y(\rho_2)$  is a symmetric function about this line provided the true mole fraction and the a priori profiles have the same shape in the troposphere. So,  $e_2$  depends on the amplitude of the first term, which is the inhomogeneity of the averaging kernel in the troposphere, and the symmetry of the second term. Similar
- 20 arguments can be applied to  $e_1$ . The difference between the stratospheric and tropospheric parts of the averaging kernel does not contribute to the error term in Eq. (23). In

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this sense the effect of the averaging kernel is removed since in our calculation the atmosphere is viewed as consisting of only two layers, the stratosphere and troposphere. In addition the equation accounting for the averaging kernel effect does not apply to HF because it is solely present in the stratosphere.

5 Similarly for the strategy implicitly using tropopause pressure, after taking the averaging kernel effect into account we get the following equations.

$$X_{\text{CH}_4}^{\text{trop}} = \frac{VC_{\text{CH}_4} - \gamma_{\text{CH}_4} - b\mu_y \left( VC_y - \gamma_y - \varphi_y \cdot X_y^{\text{trop}} \cdot VC_{\text{O}_2} / 0.2095 \right)}{\varphi_{\text{CH}_4} \cdot VC_{\text{O}_2} / 0.2095} \quad (25)$$

$$\varphi = \int_0^{P_s} a \frac{dp}{mg} / \int_0^{P_s} \frac{dp}{mg} \quad (26)$$

$$\mu = \int_0^{P_t} a_{\text{CH}_4} \left( x_t - x_t^{\text{trop}} \right) \frac{dp}{mg} / \int_0^{P_t} a \left( x_t - x_t^{\text{trop}} \right) \frac{dp}{mg} \quad (27)$$

10 For calculation of the coefficients  $\varphi$  and  $\mu$ , the true mole fraction profiles of  $\text{N}_2\text{O}$  and HF are replaced by the GFIT a priori profile, and in the case of  $\text{N}_2\text{O}$ , the a priori profile is scaled to fit the tropospheric  $\text{N}_2\text{O}$  mole fraction we assumed before.  $x_y^{\text{trop}}$  is replaced by  $X_{\text{N}_2\text{O}}^{\text{trop}}$  for  $\text{N}_2\text{O}$  or set to zero for HF.

15 To compare the derived tropospheric column-averaged  $\text{CH}_4$  mole fraction with in situ measurements, the measured  $\text{CH}_4$  profiles need to be integrated. At the same time, the averaging kernel of the FTS measurements needs to be taken into account. For our purpose only the tropospheric profile is important, and here we are only considering the case of the strategy implicitly using tropopause pressure. After replacing the total column in the right side of Eq. (25) by the right side of Eq. (10), assuming the coefficient defined by Eq. (27) accurately replaces the averaging kernels of  $\text{N}_2\text{O}$  or HF with ones of  $\text{CH}_4$ , and applying Eq. (1) in stratospheric part, it can then be seen that the effect of

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averaging kernel can be represented as:

$$X_{\text{CH}_4}^{\text{trop}} = \frac{\int_{P_t}^{P_s} a_{\text{CH}_4} x_t \frac{dp}{mg}}{\int_{P_t}^{P_s} a_{\text{CH}_4} \frac{dp}{mg}} \quad (28)$$

to integrate the aircraft data, with  $x_t$  simply replaced by the in situ profile.

### 3.4 Taking calibration factors into account

5 The derivations above are based on the total columns of  $\text{CH}_4$ ,  $\text{N}_2\text{O}$  and  $\text{HF}$ , but the total columns directly retrieved from the spectra include errors arising from spectroscopy imperfections and instrumental effects. The final TCCON products are the dry air column averaged mole fraction  $X_{\text{CH}_4}$ ,  $X_{\text{N}_2\text{O}}$  and  $X_{\text{HF}}$ , which have been corrected by air mass independent and air mass dependent calibration factors to account for such errors. These  
 10 corrections should be taken into account for this work. For the strategy explicitly using tropopause pressure, after combining Eqs. (15) and (16) the final equation becomes,

$$X_{\text{CH}_4}^{\text{trop}} = \frac{\alpha_{\text{CH}_4}}{f} \left\{ X_{\text{CH}_4} - \left[ a(1-f) + b \cdot \beta_y \left( X_y - X_y^{\text{trop}} \cdot f \cdot \alpha_y^{-1} - \frac{Y_y}{\text{VC}_{\text{air}}} \right) \right] \beta_{\text{CH}_4}^{-1} - \frac{Y_{\text{CH}_4}}{\text{VC}_{\text{air}}} \right\}, \quad (29)$$

where,  $f$  is the fraction of the tropospheric dry air column in the total dry air column, and  $\text{VC}_{\text{air}}$  is the summation of the left hand sides of Eqs. (5) and (6). For the strategy  
 15 implicitly using tropopause pressure, the Eq. (26) can be written as:

$$X_{\text{CH}_4}^{\text{trop}} = \frac{1}{\varphi_{\text{CH}_4}} \left[ X_{\text{CH}_4} - \frac{Y_{\text{CH}_4}}{\text{VC}_{\text{air}}} - b \cdot \mu_y \left( X_y - \frac{Y_y}{\text{VC}_{\text{air}}} - \varphi_y \cdot X_y^{\text{trop}} \right) \right] \quad (30)$$

The air mass independent calibration factors are taken as those used throughout TCCON (Wunch et al., 2010). These factors have been re-evaluated by Geibel (2012) based on European sites, but this reevaluation is not taken into account because it has  
 20 not been applied to the current TCCON release.

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## 4 Results

To test the method described in Sect. 3, data from four TCCON sites at Spitsbergen, Orléans, Bialystok and Darwin are used. Figure 4 presents the comparison for the two strategies described in Sect. 3 at Spitsbergen in the case of  $\text{N}_2\text{O}$ , since only at this site do the two methods produce a significant difference. The method explicitly using tropopause pressure results in a larger value in comparison with in situ data in winter time. This might arise from an error in the tropopause pressure derived from the NCEP temperature profile. During wintertime the tropopause is lower and this method is more sensitive to such an error. The seasonal cycle amplitude in tropospheric column-averaged  $\text{CH}_4$  mole fraction resulting from the method implicitly using tropopause pressure is weaker than that observed in collocated in situ data. It is not clear how the in situ data differ from tropospheric column-averaged value at this site. In the case of HF, the method explicitly using tropopause pressure also produce higher value, but the difference is only around 10 ppb around. In the iteration process of the method explicitly using tropopause pressure, the vertical distribution of  $\text{CH}_4$  in the troposphere should be known to derive  $\text{CH}_4$  mole fraction at tropopause from the tropospheric column-averaged concentration. The GFIT a priori distribution is assumed here. So, for all the following results, the strategy implicitly using tropopause pressure is applied.

### 4.1 Comparison between the $\text{N}_2\text{O}$ and HF methods and in situ data

Figures 5–8 show the results for Spitsbergen, Orléans, Bialystok and Darwin. We compare to in situ data from NOAA at Spitsbergen, and the low aircraft data at Orléans and Bialystok. These profiles have been extended into whole troposphere as described in Sect. 2.2, and then integrated to produce a tropospheric column-averaged  $\text{CH}_4$  mole fraction. At all sites with in situ data available for comparison the results using  $\text{N}_2\text{O}$  are closer to the in situ measurements than when using HF. The difference between the results using  $\text{N}_2\text{O}$  and HF has both seasonal and site dependence. At Spitsbergen the

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0.20% respectively in the case of HF. So the method using HF produces larger uncertainties, especially at Darwin. Also the uncertainty of the method using HF has a stronger H<sub>2</sub>O dependence. This is because the retrieval of HF column suffers strong interference from H<sub>2</sub>O, and so does the derived tropospheric column-averaged CH<sub>4</sub> mole fraction.

## 6 Conclusions

In this paper, we propose using N<sub>2</sub>O to correct for the stratospheric contribution to the total column of CH<sub>4</sub> in order to derive a tropospheric column-averaged CH<sub>4</sub> mole fraction. This method is applied to four TCCON sites data. At Spitsbergen and Orléans, the tropospheric CH<sub>4</sub> derived using N<sub>2</sub>O and HF are compared with surface flask measurements and low aircraft profiles data, respectively. At both sites, the results using N<sub>2</sub>O agree better with in situ measurements than the HF derived results. Uncertainty analysis reveals that N<sub>2</sub>O method results in smaller uncertainty than HF at all sites. The mean relative standard deviations are 0.23% and 0.52% for the methods using N<sub>2</sub>O and HF, respectively. Especially, at Darwin the HF method produces much larger uncertainty (0.93% compared with 0.15% of N<sub>2</sub>O method), which clearly indicates a dependence on H<sub>2</sub>O that is absent for the N<sub>2</sub>O method. This N<sub>2</sub>O method has also been compared with aircraft profiles at three sites, and the result reveals that N<sub>2</sub>O method has better inter-site consistency. The sensitivity of the derived tropospheric CH<sub>4</sub> to the assumed tropospheric N<sub>2</sub>O mole fraction is 4 ~ 5 ppb per 2 ppb. Further work can be done to represent N<sub>2</sub>O mole fraction in troposphere more realistically.

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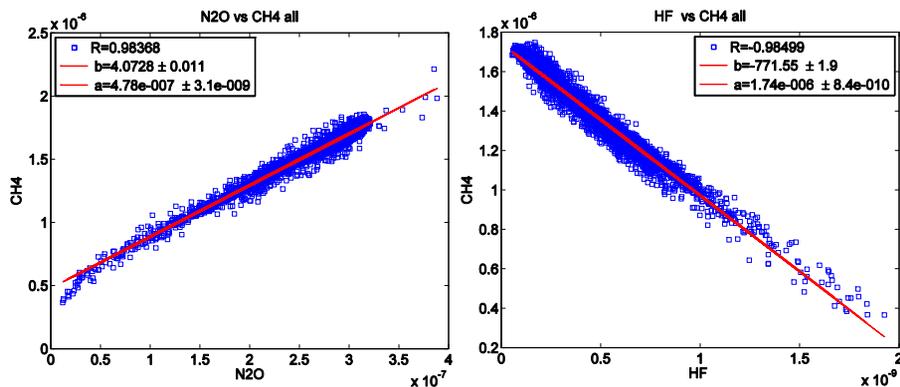
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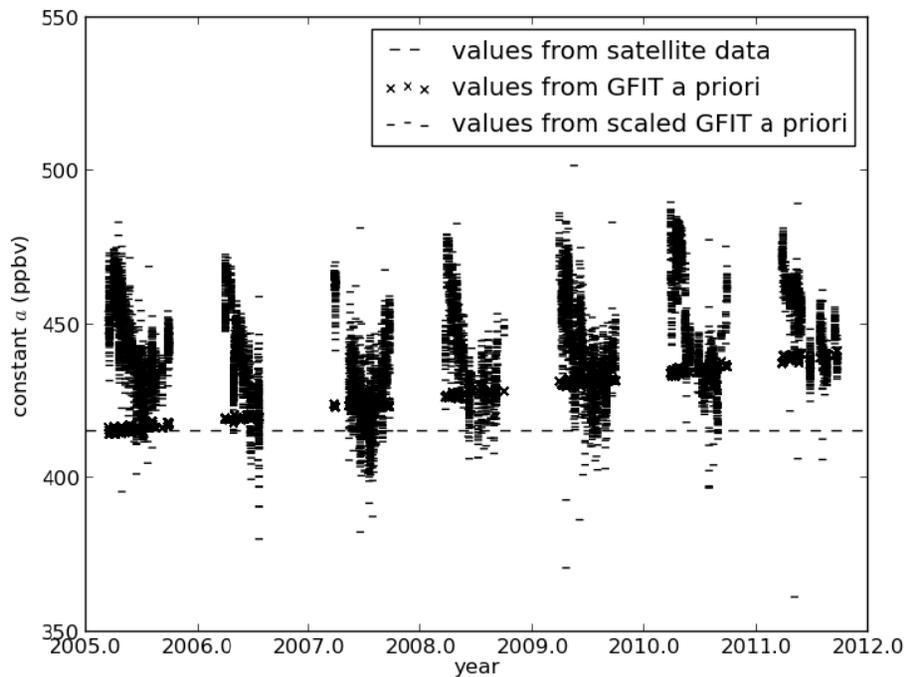
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**Fig. 1.** Correlations between the stratospheric mole fractions of N<sub>2</sub>O (right) and HF (left) with CH<sub>4</sub> on a global scale. Correlation coefficient, slope and intercept are indicated in the legend.

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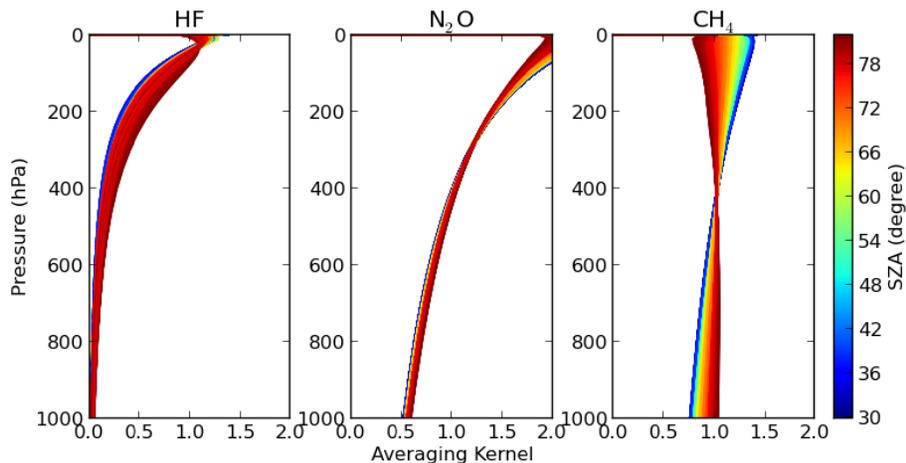


**Fig. 2.** Comparison between constant  $a$  derived from original and scaled GFIT a priori, ACE-FTS satellite data at Spitsbergen.

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**Fig. 3.** The averaging kernels of HF, N<sub>2</sub>O and CH<sub>4</sub> at Bialystok for all spectra from 2010. The colors indicate the solar zenith angle of the corresponding measurements.

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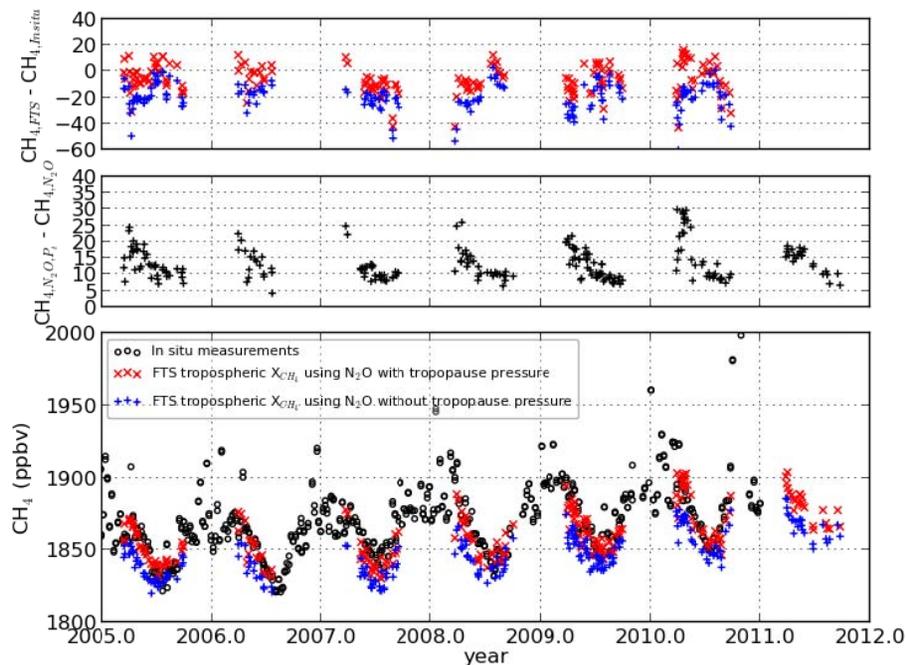
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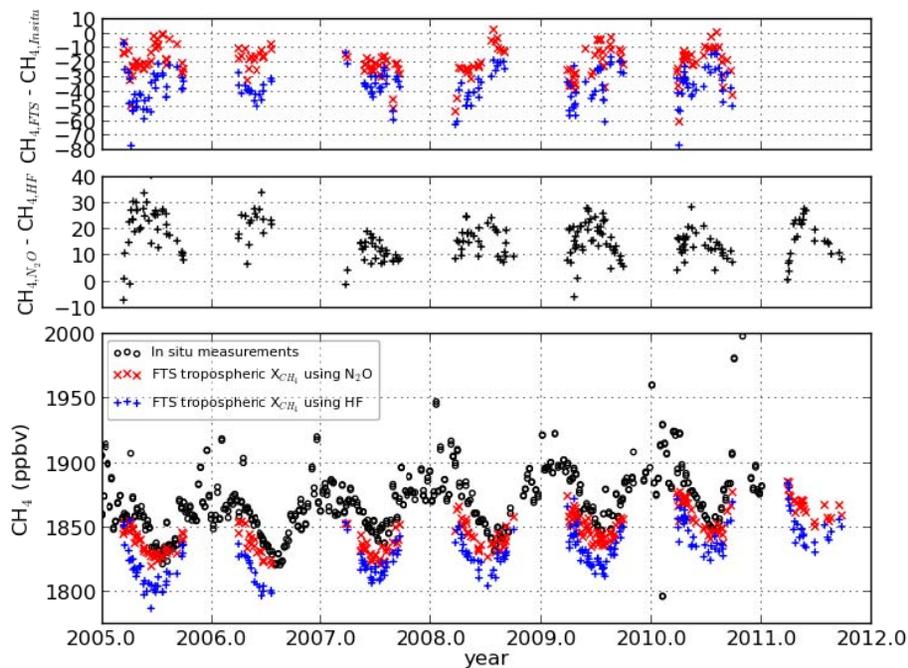
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**Fig. 4.** Comparison results of two methods at Spitsbergen. The red points correspond to the tropospheric column-averaged CH<sub>4</sub> mole fraction derived from N<sub>2</sub>O and explicitly using tropopause pressure, the blue to those derived from N<sub>2</sub>O and implicitly using tropopause pressure and the open circles are in situ CH<sub>4</sub> data measured at Zeppelin mountain provided by NOAA (Dlugokencky et al., 2012). The upper panel shows the difference between the in situ CH<sub>4</sub> and the tropospheric column-averaged CH<sub>4</sub> mole fractions, the middle panel is the difference between results using two methods.

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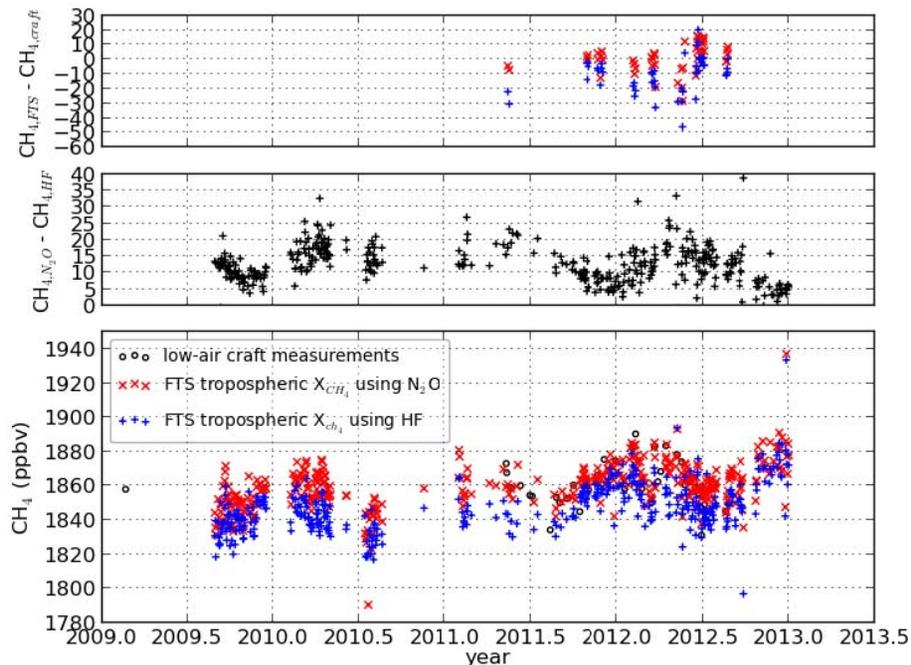


**Fig. 5.** Results at Spitsbergen, the red points correspond to the tropospheric column-averaged CH<sub>4</sub> mole fraction derived from N<sub>2</sub>O, the blue to those derived using HF and the open circles are in situ CH<sub>4</sub> data measured at Zeppelin mountain. The upper panel shows the difference between the in situ and tropospheric column-averaged CH<sub>4</sub> mole fractions, the middle panel is the difference between the results using N<sub>2</sub>O and HF.

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**Fig. 6.** Same as Fig. 5 except for the Orléans site and with the black points in the lower panel representing tropospheric column-averaged  $\text{CH}_4$  mole fractions derived from low aircraft flights at this site.

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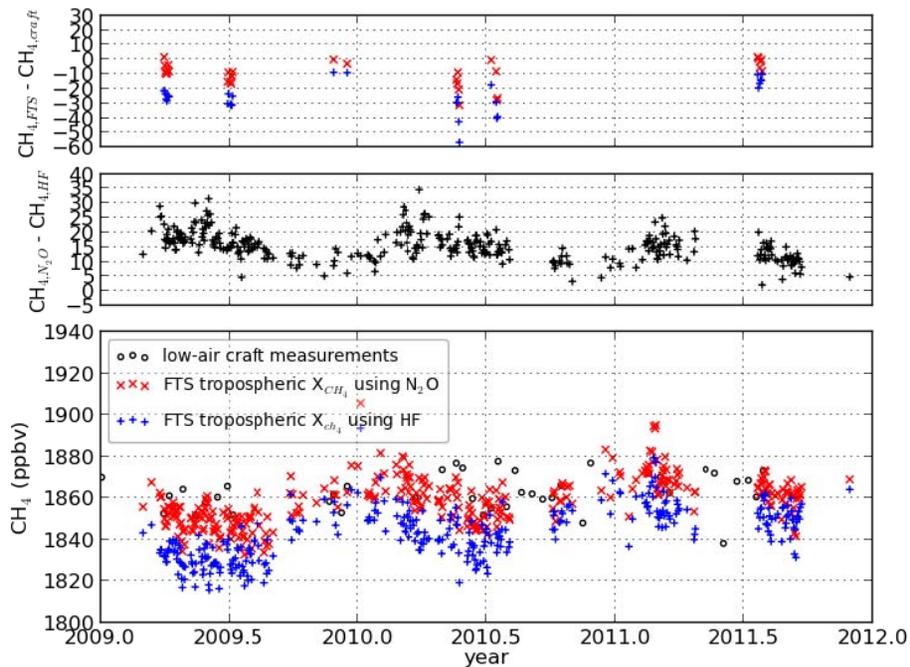


Fig. 7. Same with Fig. 6 except for Bialystok.

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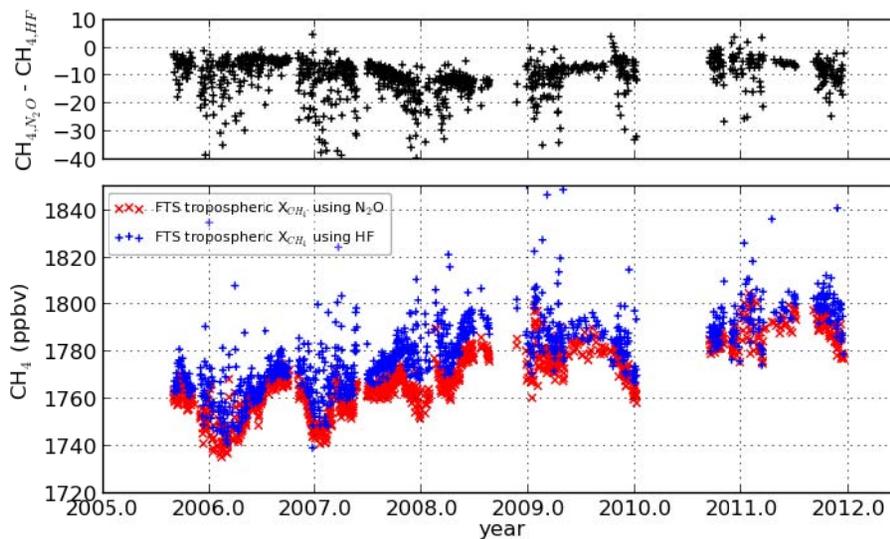
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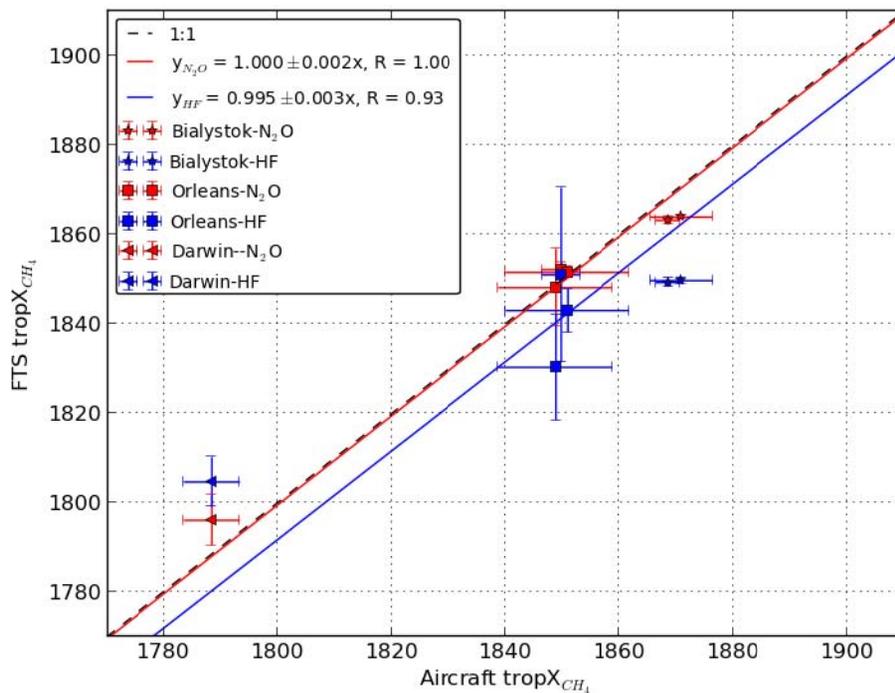
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**Fig. 9.** Comparison results with aircraft data. The aircraft profiles are smoothed using GFIT averaging kernels in troposphere using Eq. (28). The FTS data are averaged through aircraft measurements periods, and the error bars of FTS data are standard deviations of these averaged data.

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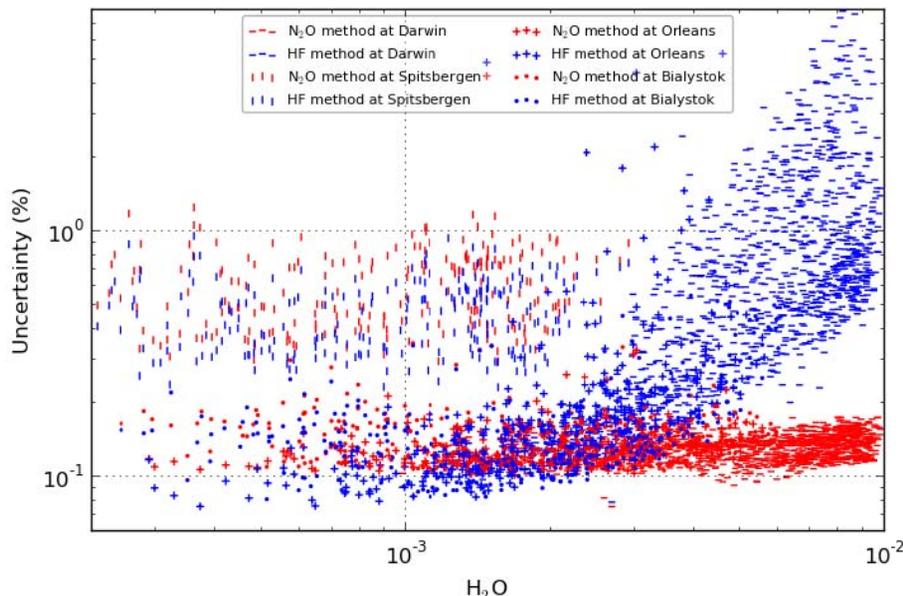
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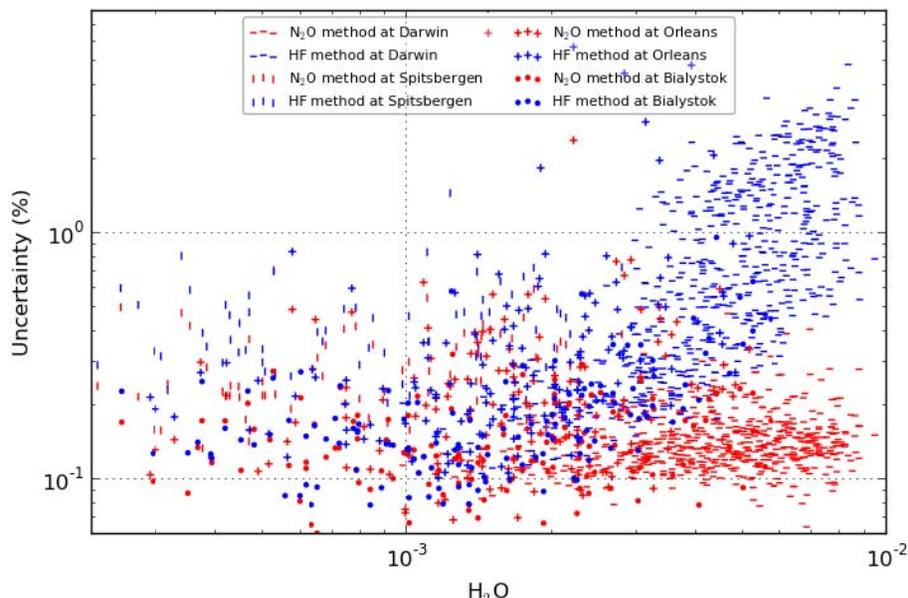


**Fig. 10.** Relative error estimation of the tropospheric column-averaged CH<sub>4</sub> mole fraction using Gaussian error propagation equation for four sites, the blue corresponds to the error for the method using HF and the red to that of method using N<sub>2</sub>O.

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**Fig. 11.** Same as Fig. 9, except for that the relative error is estimated as the standard deviation of daily mean tropospheric CH<sub>4</sub>.

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